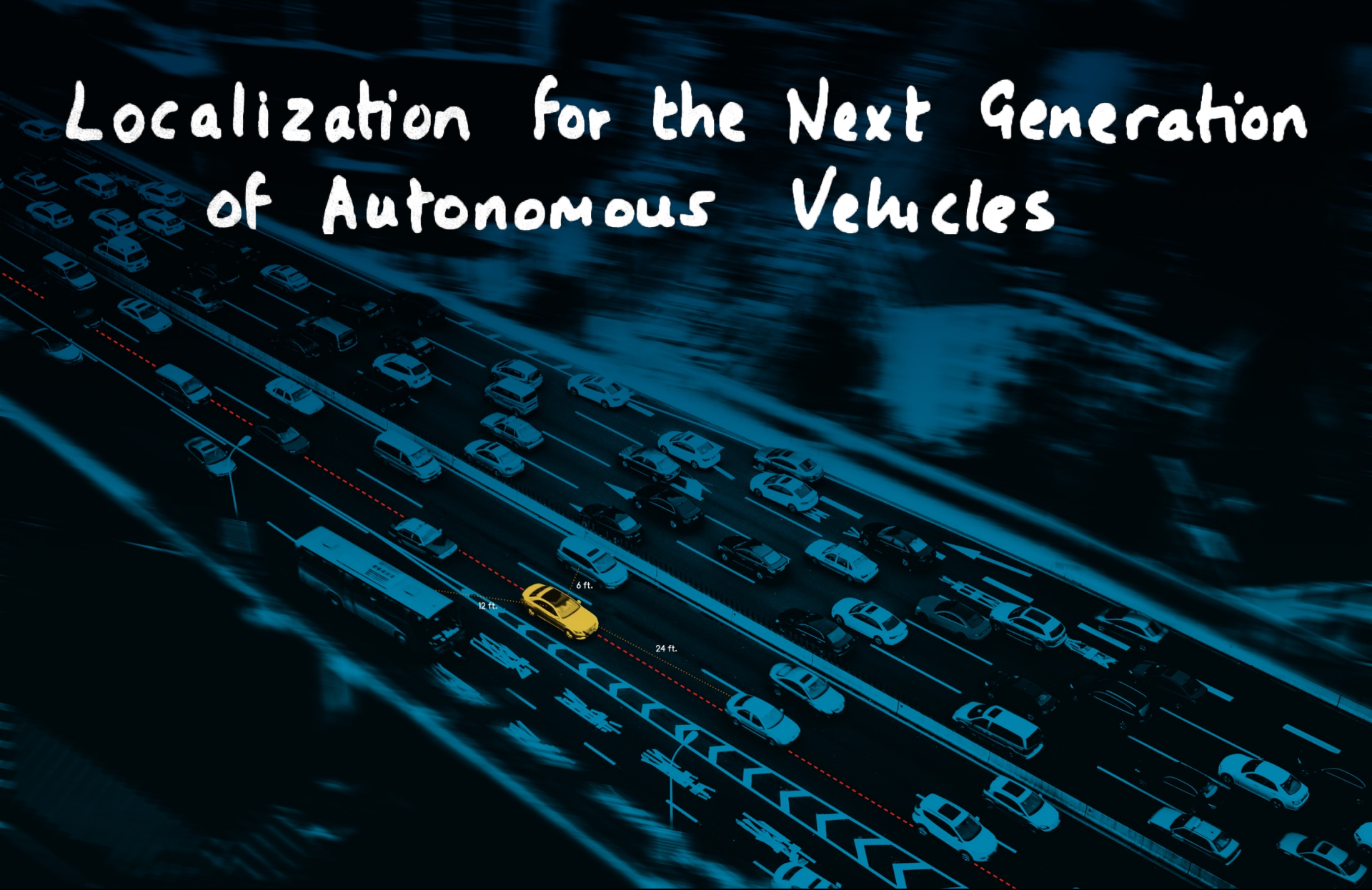


# Localization for the Next Generation of Autonomous Vehicles



Fergus Noble CTO



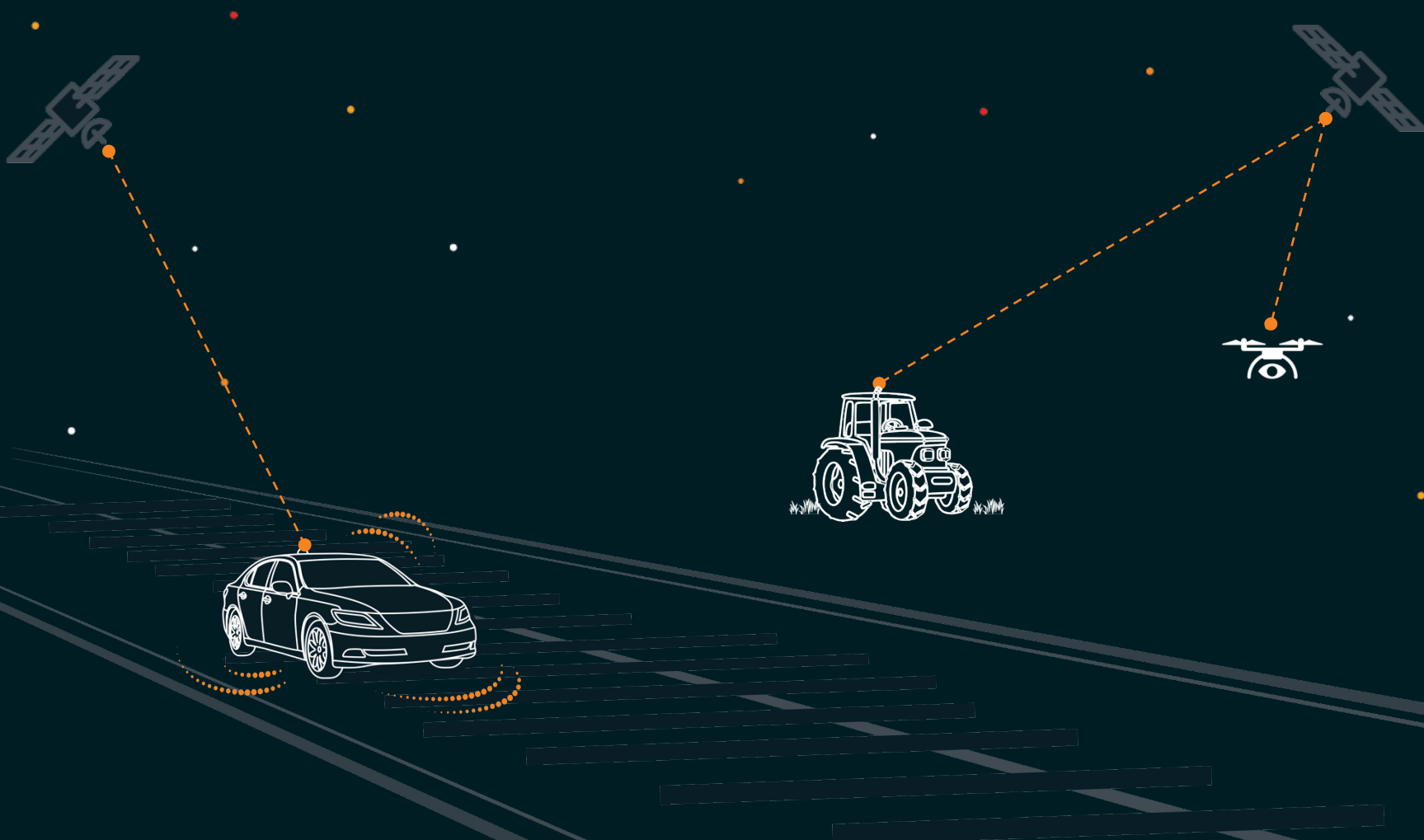
- Autonomy is arriving



- Autonomy is arriving
- Autonomous vehicles need centimeter positioning to navigate

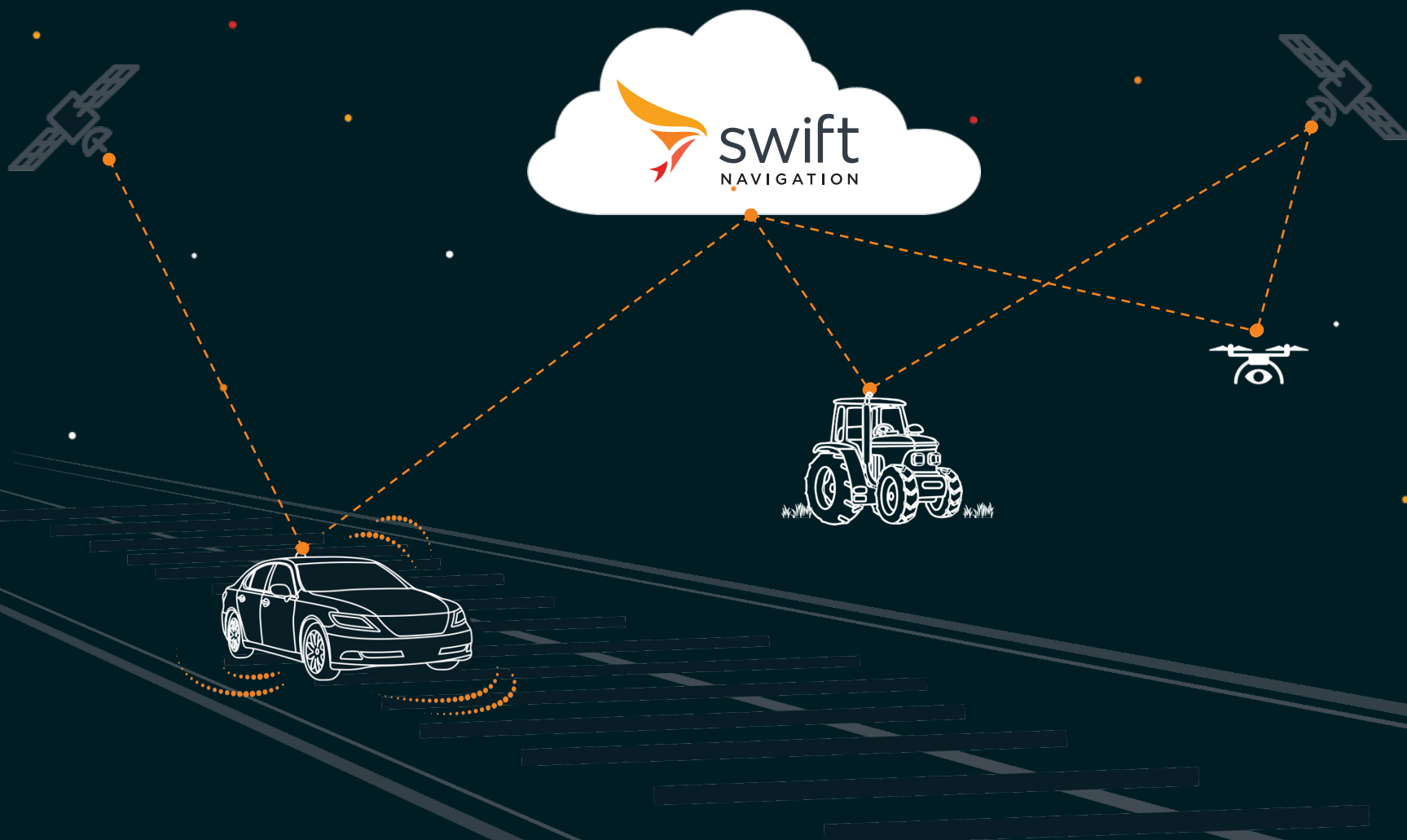


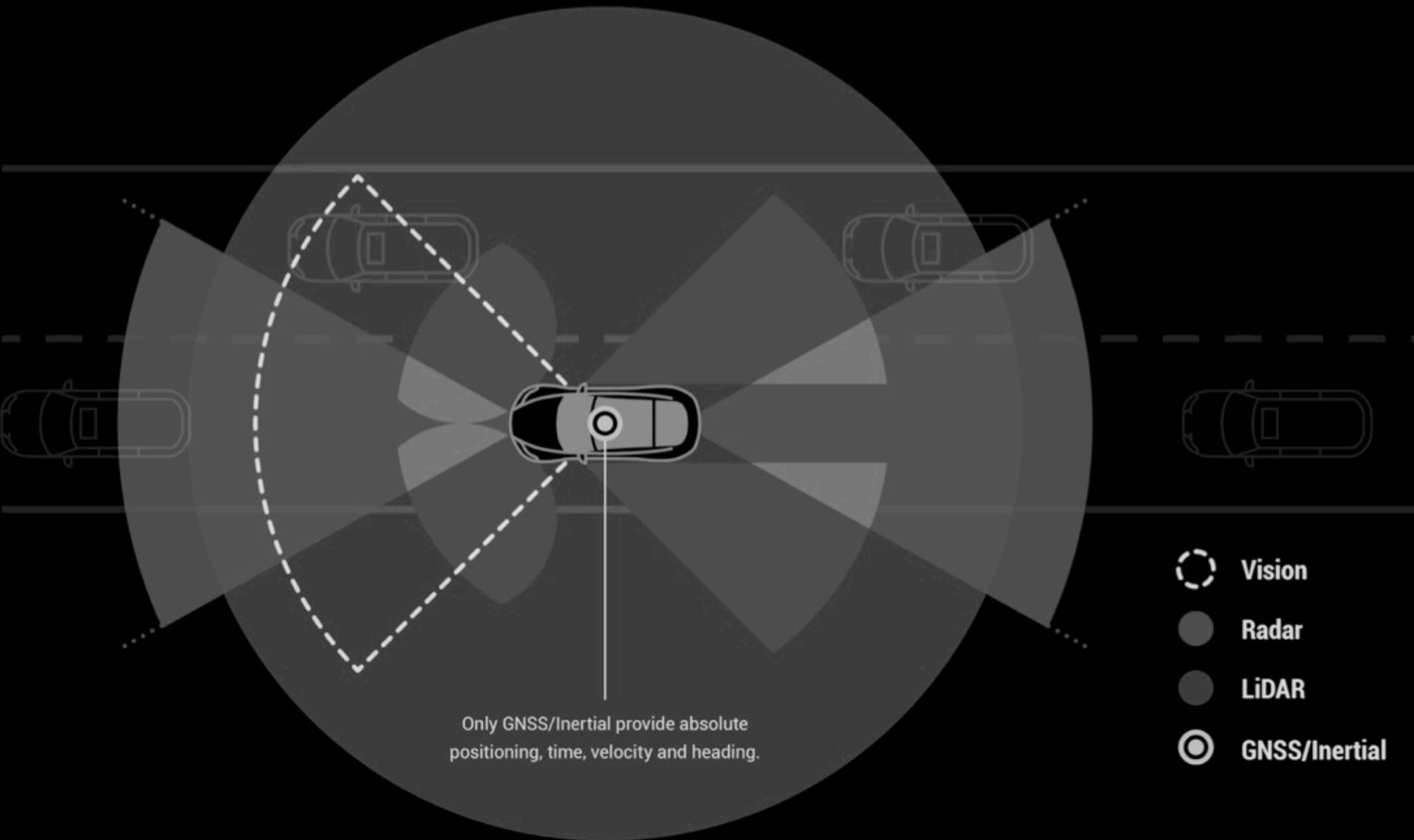
- Autonomy is arriving
- Autonomous vehicles need centimeter positioning to navigate
- GPS is the only way to acquire absolute location, but it is inaccurate





- Autonomy is arriving
- Autonomous vehicles need centimeter positioning to navigate
- GPS is the only way to acquire absolute location, but it is inaccurate
- An advanced centimeter-accurate GPS is required for autonomy





LACK OF LANE MARKINGS



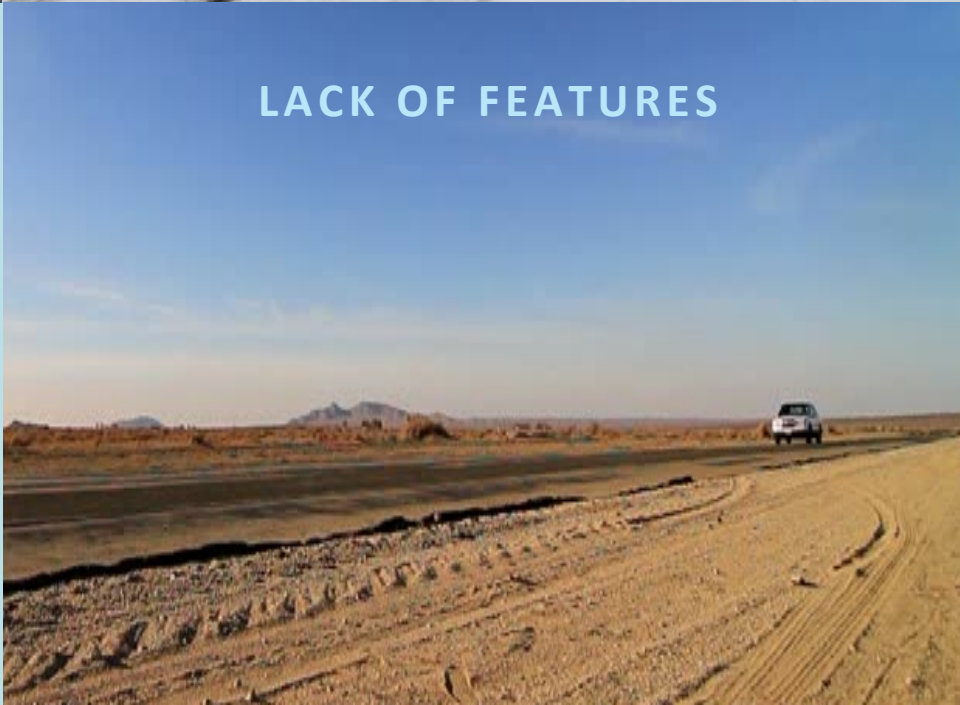
INCLEMENT WEATHER

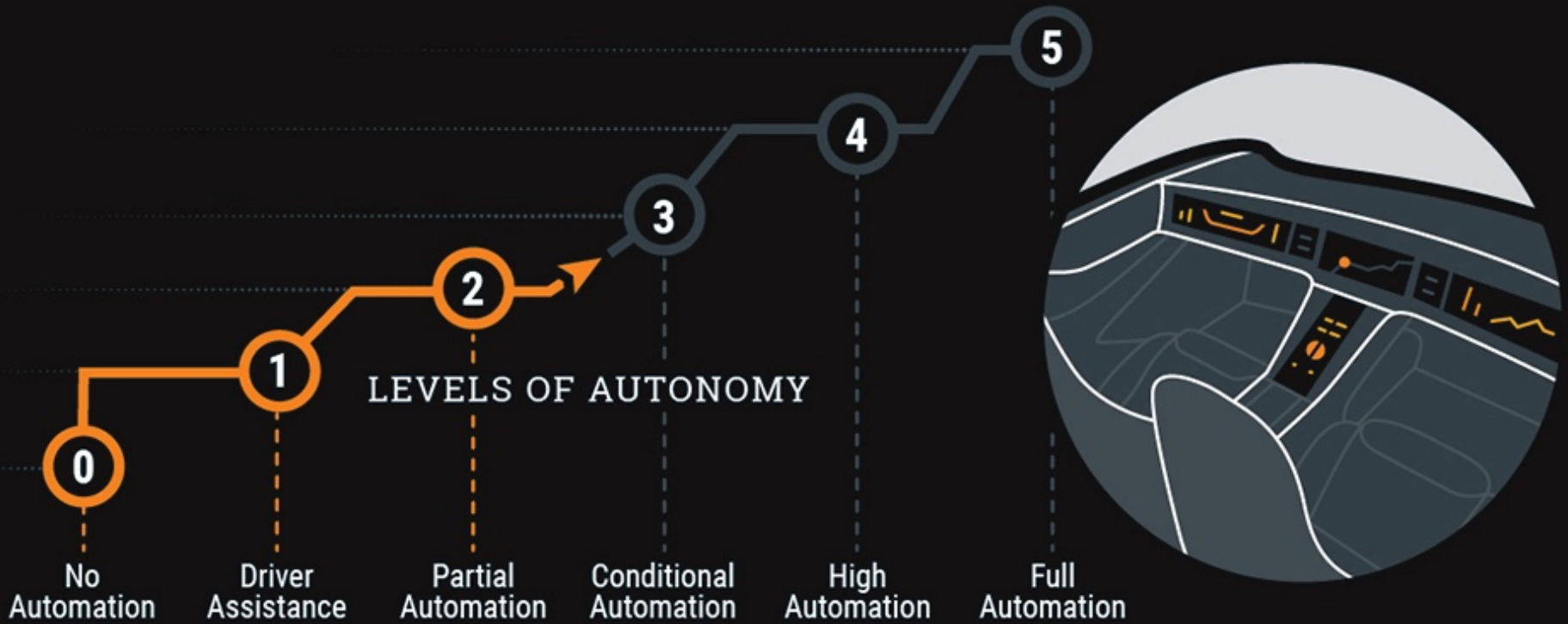


LANE AMBIGUITY



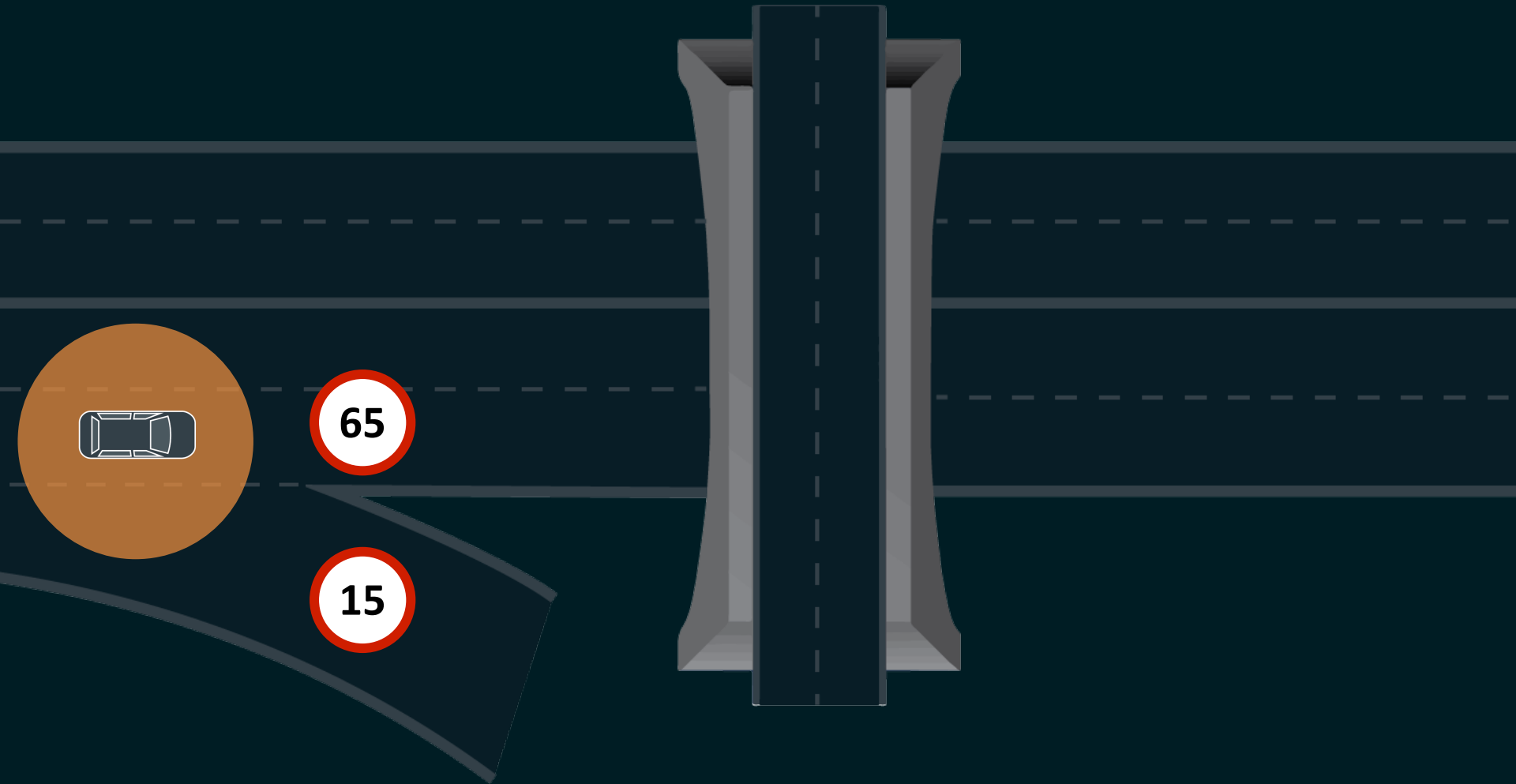
LACK OF FEATURES





# AUTONOMY REQUIRIES

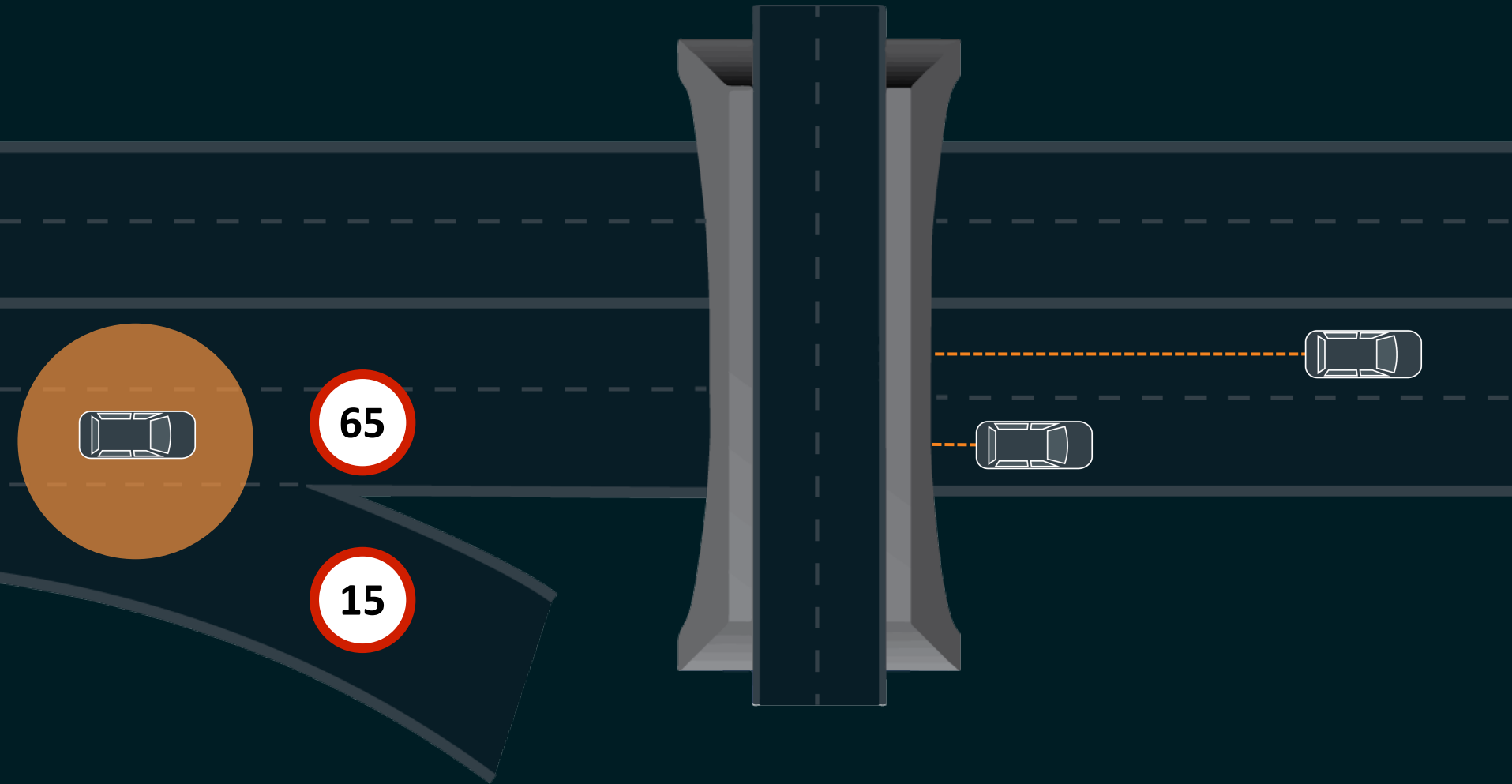
- HIGH PRECISION





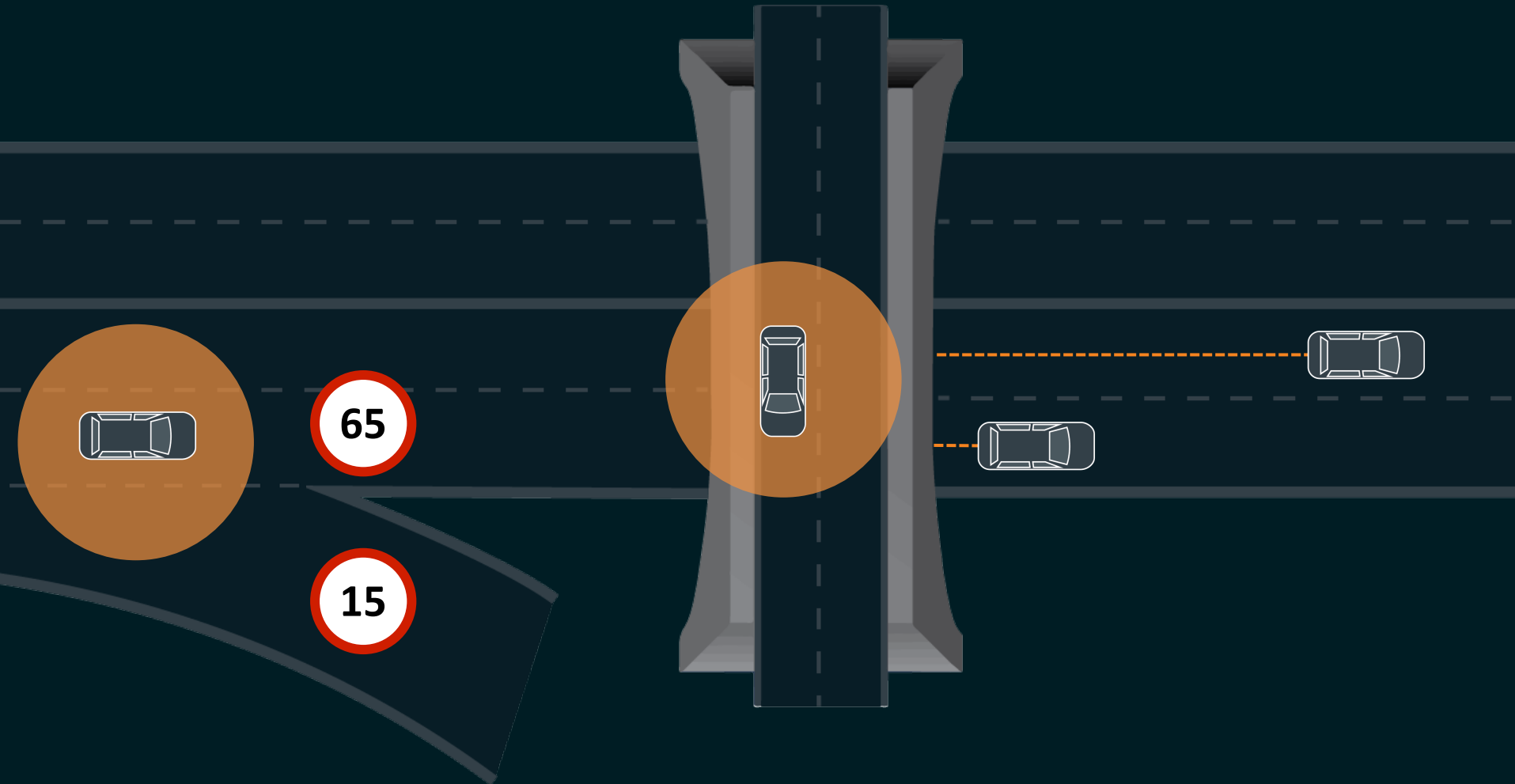
## AUTONOMY REQUIRES

- HIGH PRECISION
- AVAILABILITY



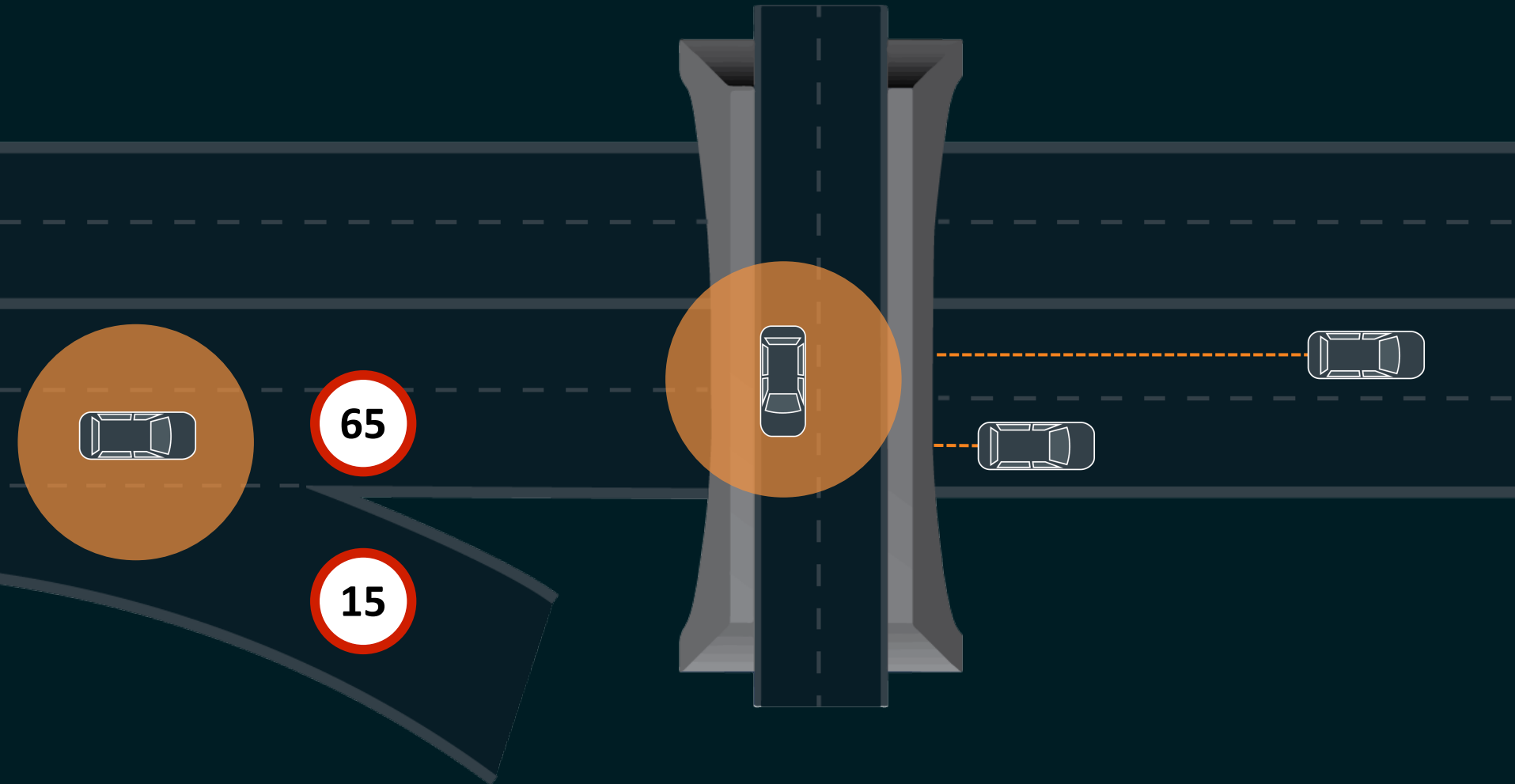
## AUTONOMY REQUIRIES

- HIGH PRECISION
- AVAILABILITY
- INTEGRITY



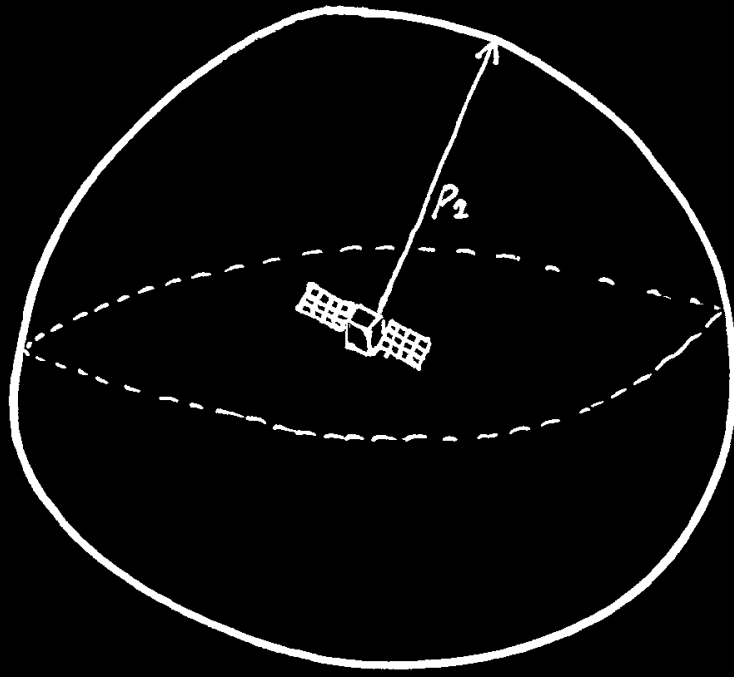
## AUTONOMY REQUIRIES

- HIGH PRECISION
- AVAILABILITY
- INTEGRITY
- LOW COST



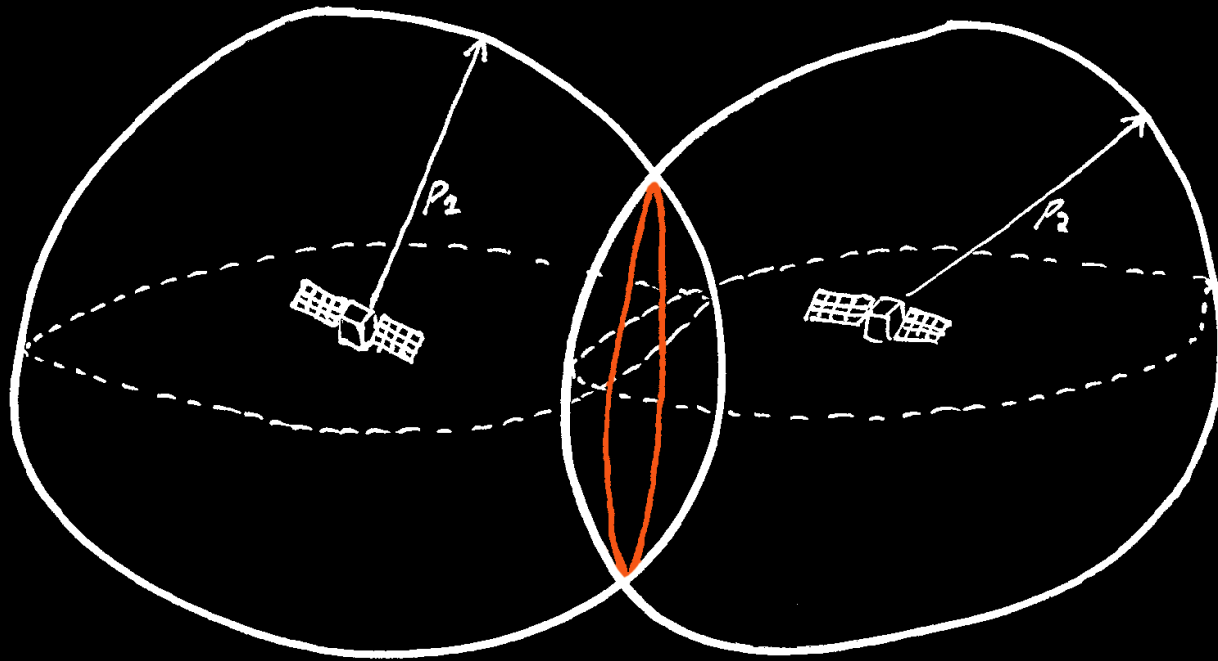
How does GPS work?

Solving for position

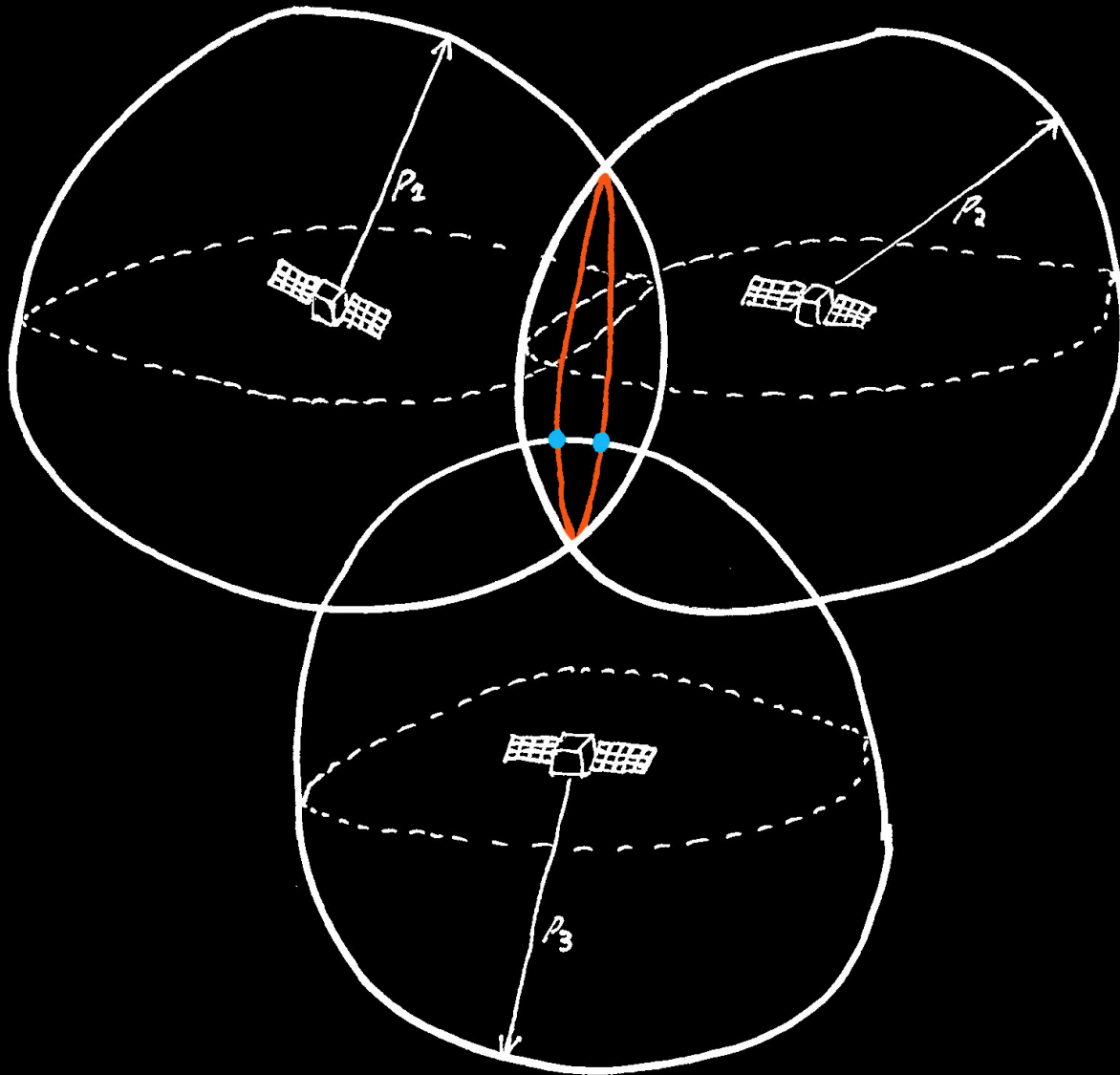




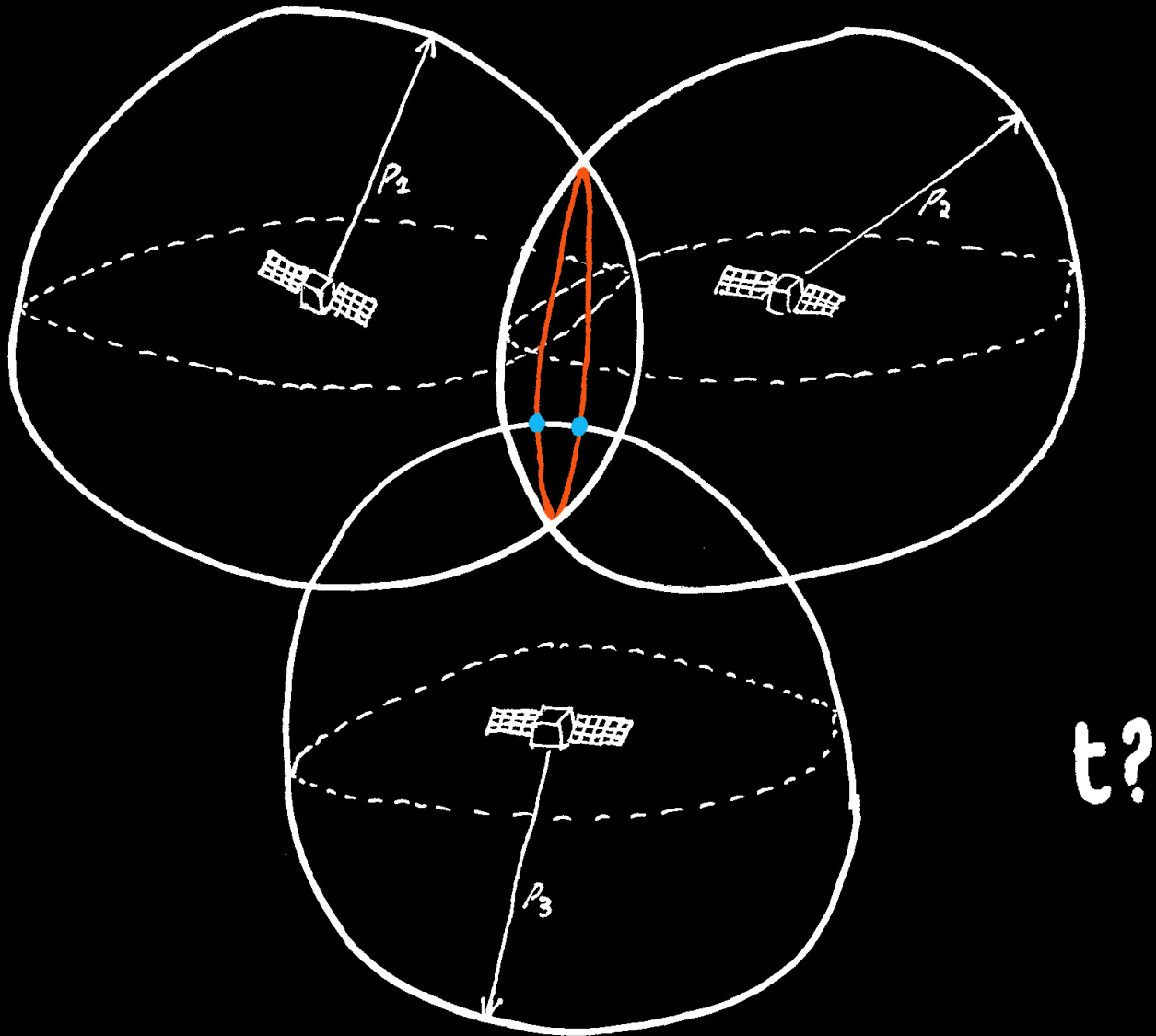
# Solving for position



# Solving for position



# Solving for position



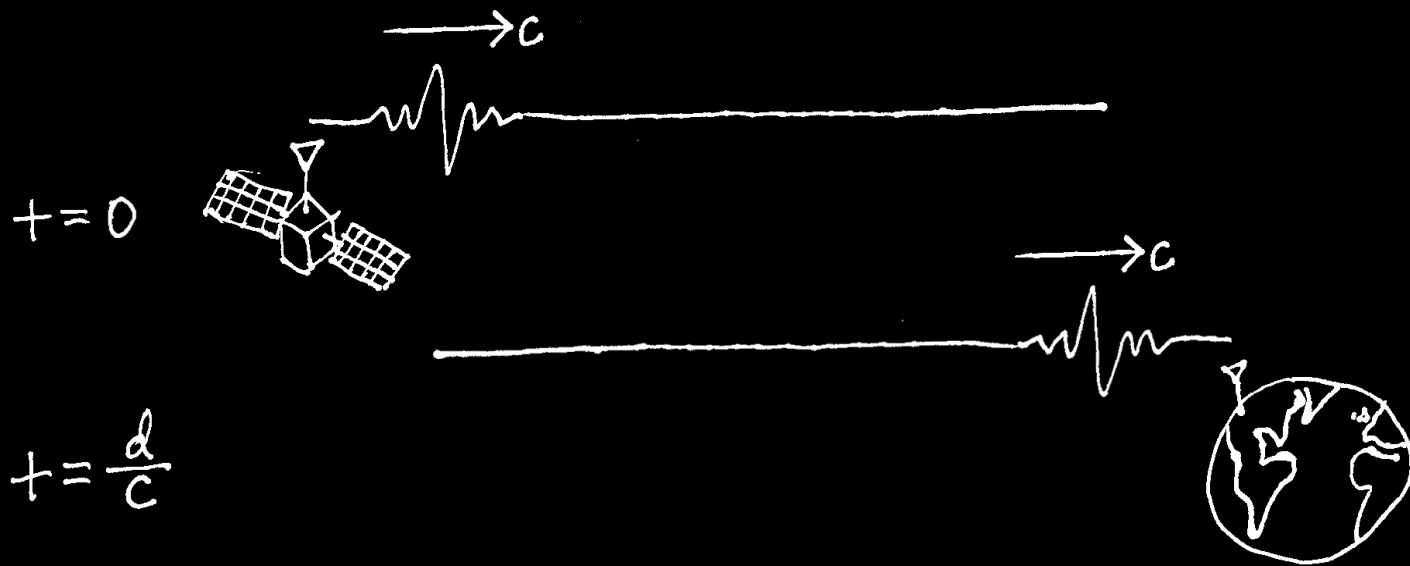
How can we measure the distance  
to the satellite?



distance  $\Leftrightarrow$  time

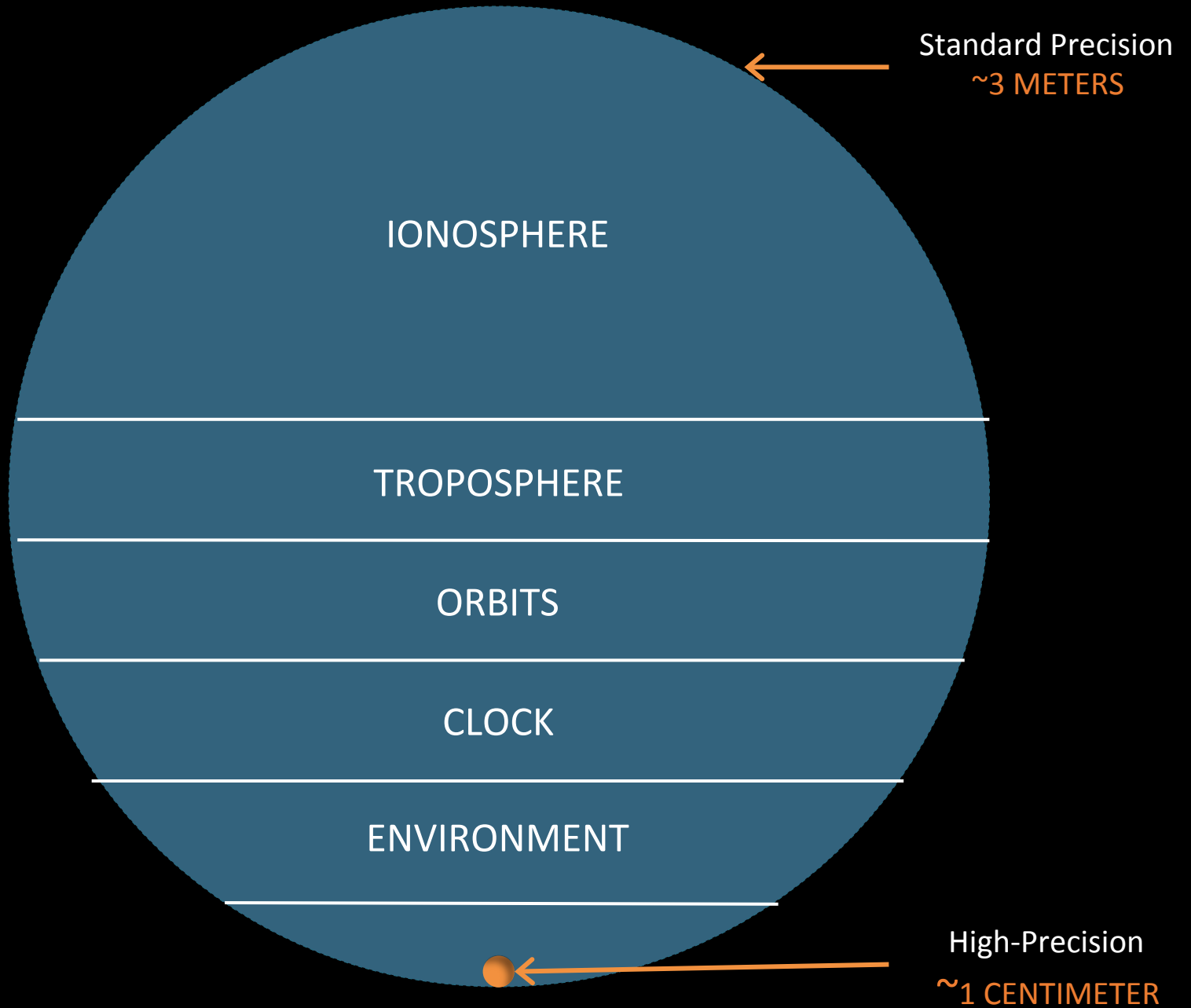
$d$   $t$

$$d = ct$$





Sources of error

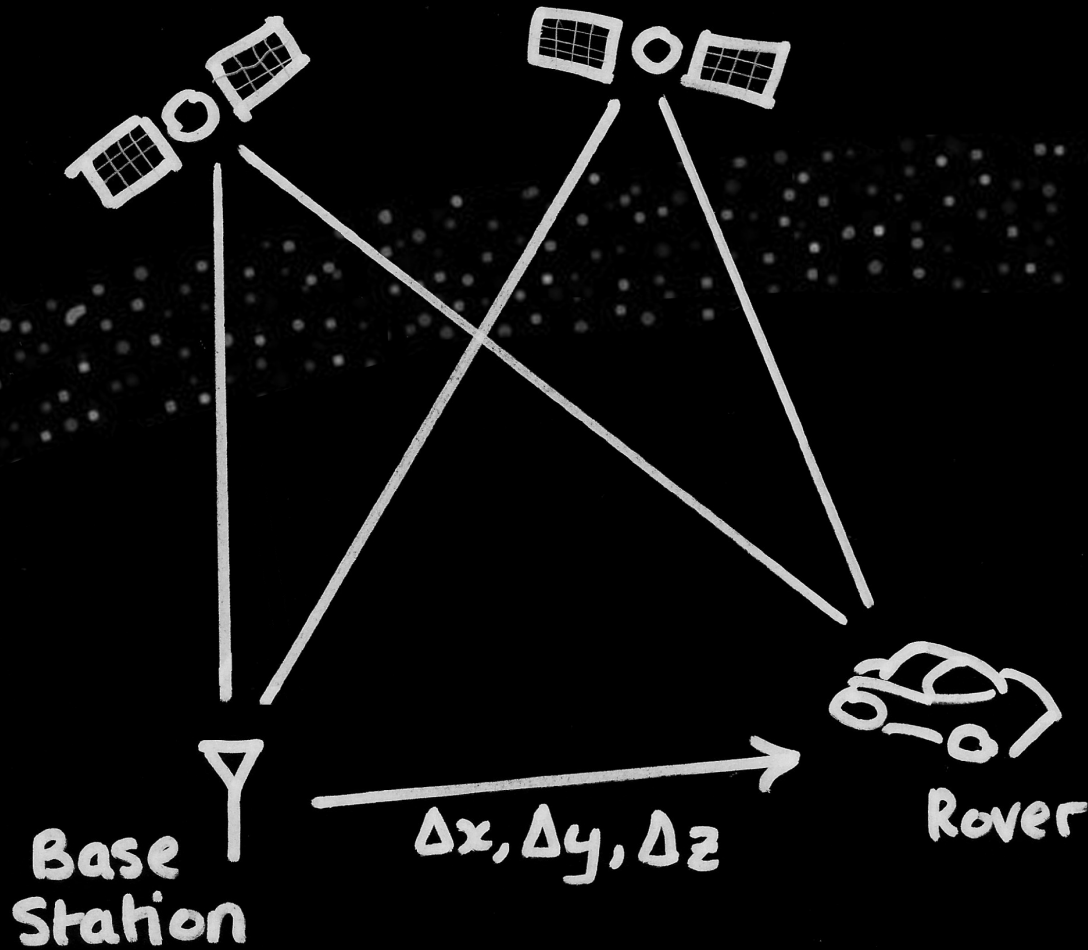


# Real Time Kinematic

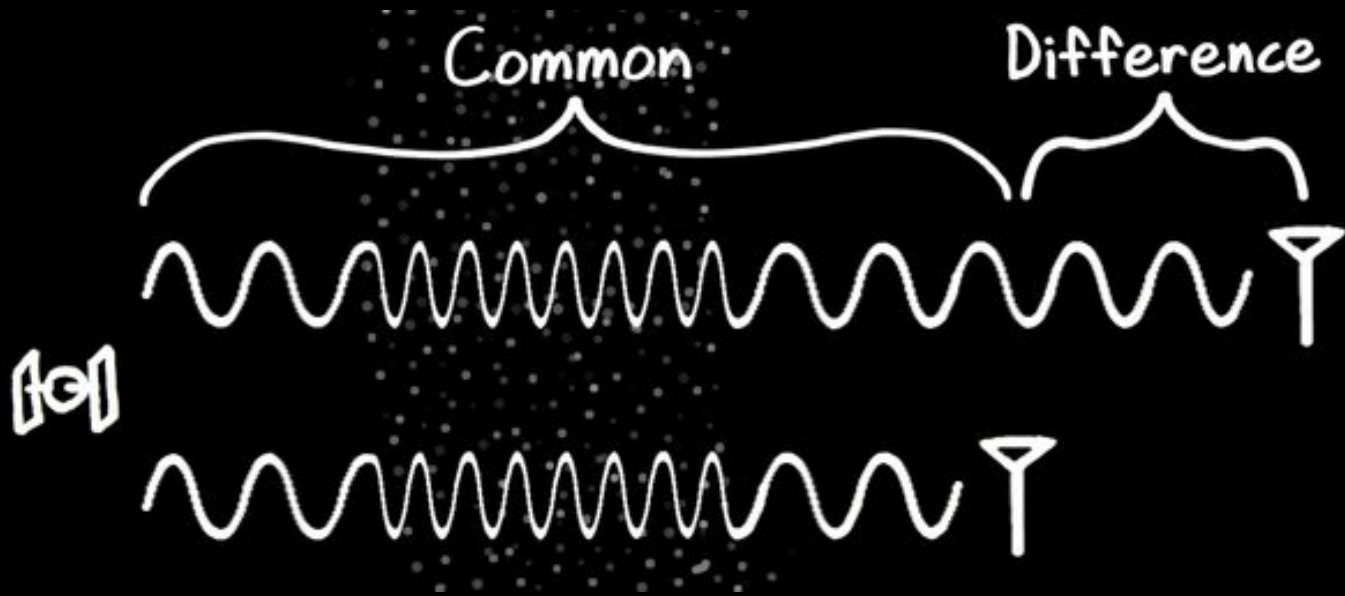


- 1) Differential
- 2) Carrier - phase

# Ionosphere

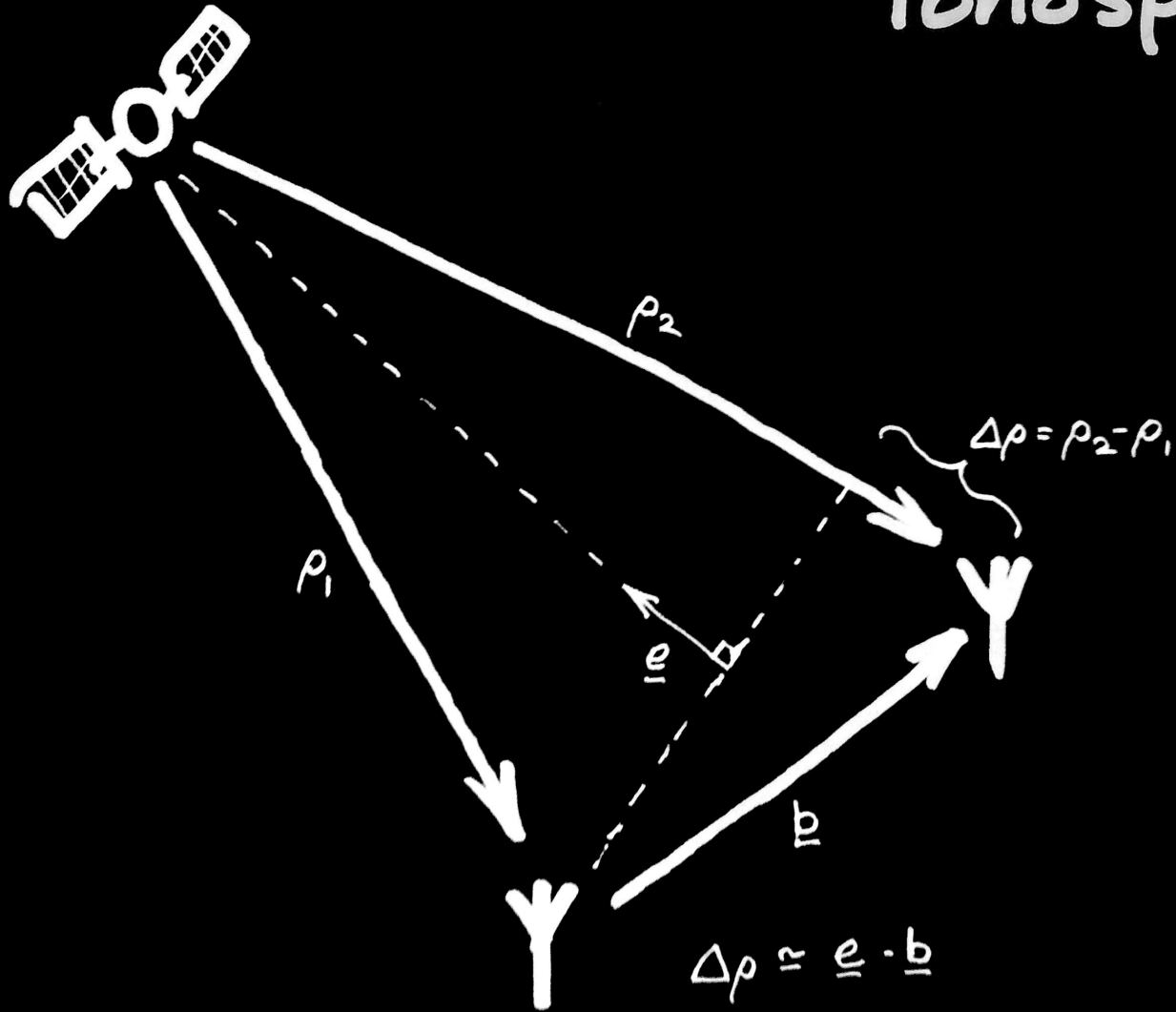


# Ionosphere

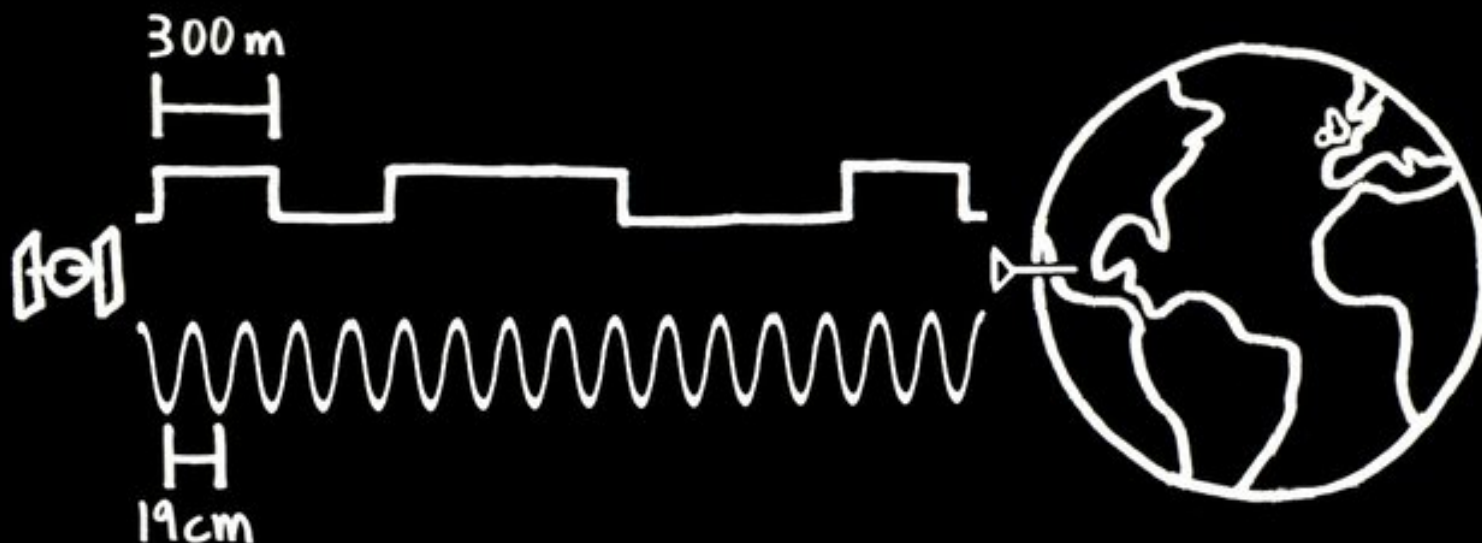




# Ionosphere

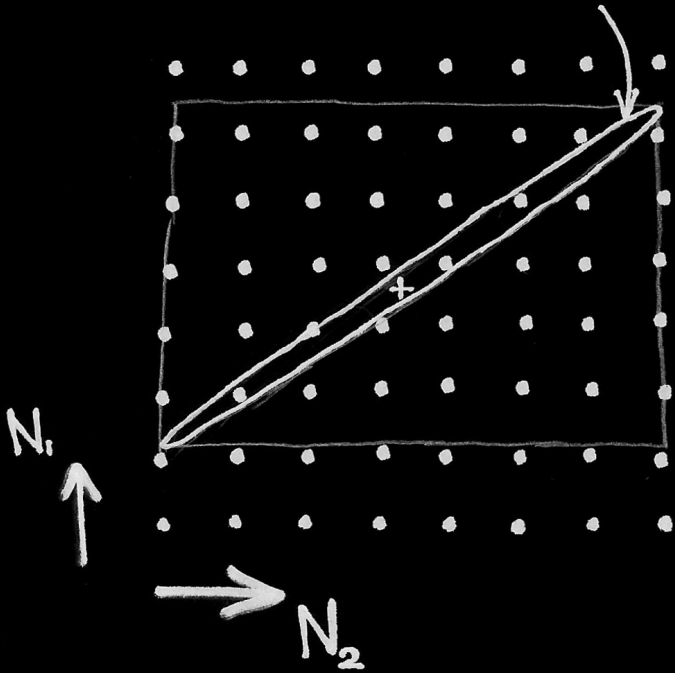


# Measurement Precision



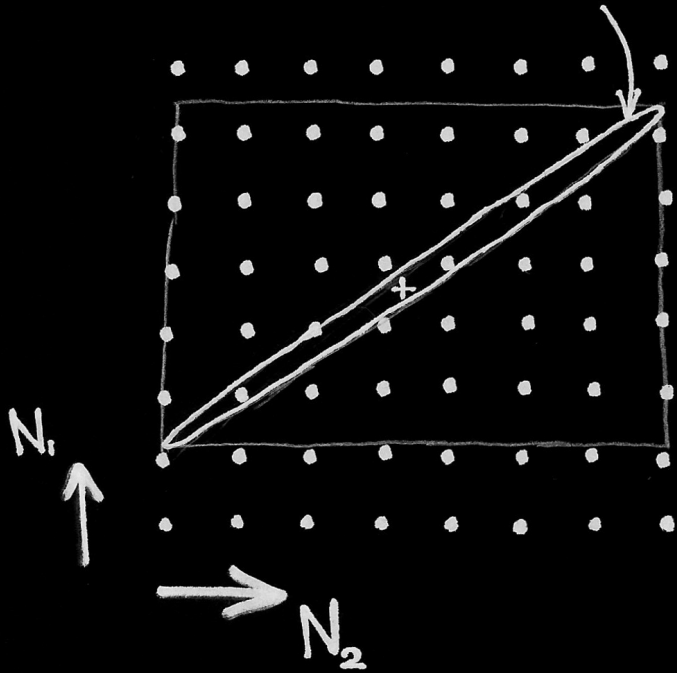
# Measurement Precision

"Float" Kalman Filter  
covariance

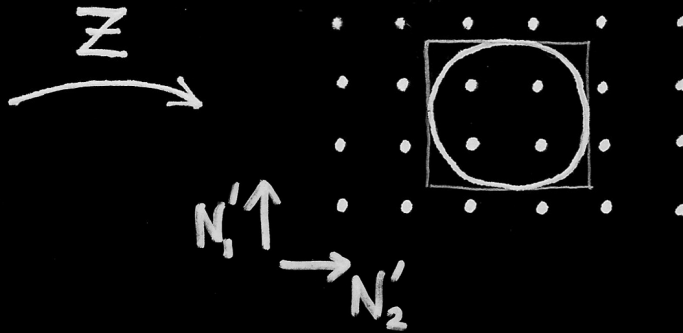


# Measurement Precision

"Float" Kalman Filter  
covariance



LAMBDA



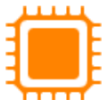
# Introducing Piksi™ Multi



Fast RTK convergence times measured in seconds, not minutes



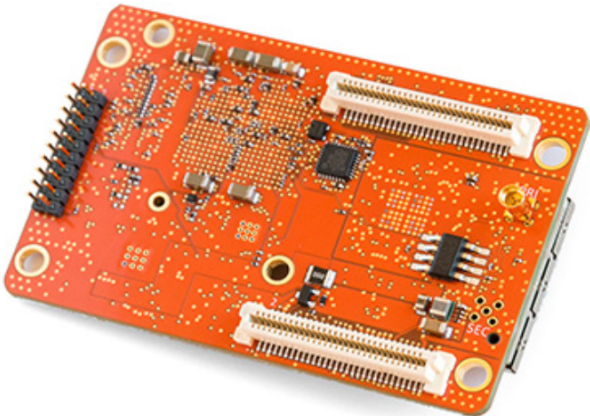
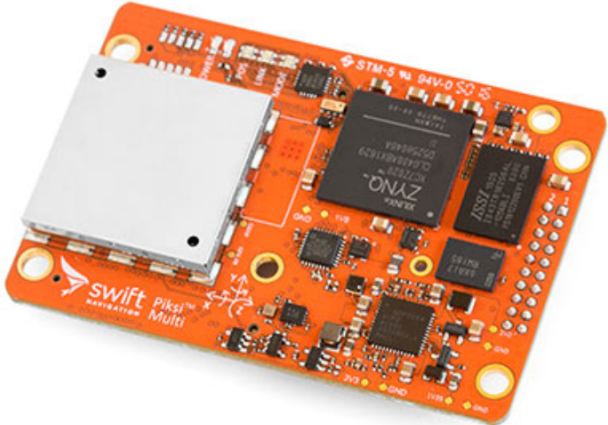
Improve results with centimeter-accurate positioning



Open platform featuring powerful FPGA & dual core processor



UART, CAN, USB & Ethernet interfaces



Breakthrough price of \$595



GPS L1/ L2  
Hardware-ready for GLONASS, BeiDou, Galileo



Small form factor compatible with common GNSS modules



Designed for rapid prototyping & ease of use

## Meet Duro

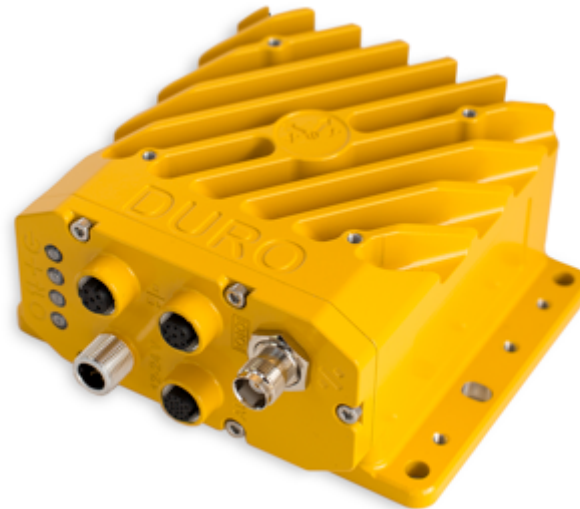
Duro is a ruggedized version of the Piksi Multi RTK GNSS receiver. Built to be tough, Duro is ideal for agricultural, robotics, maritime and outdoor industrial applications. Duro is designed for integration into existing equipment. This easy-to-deploy GNSS sensor is protected against weather, moisture, vibration, dust, water immersion and the unexpected that can occur in outdoor long-term deployments.



Centimeter-accurate  
positioning



Military-grade,  
rugged enclosure



Easy to deploy,  
ready out of the box

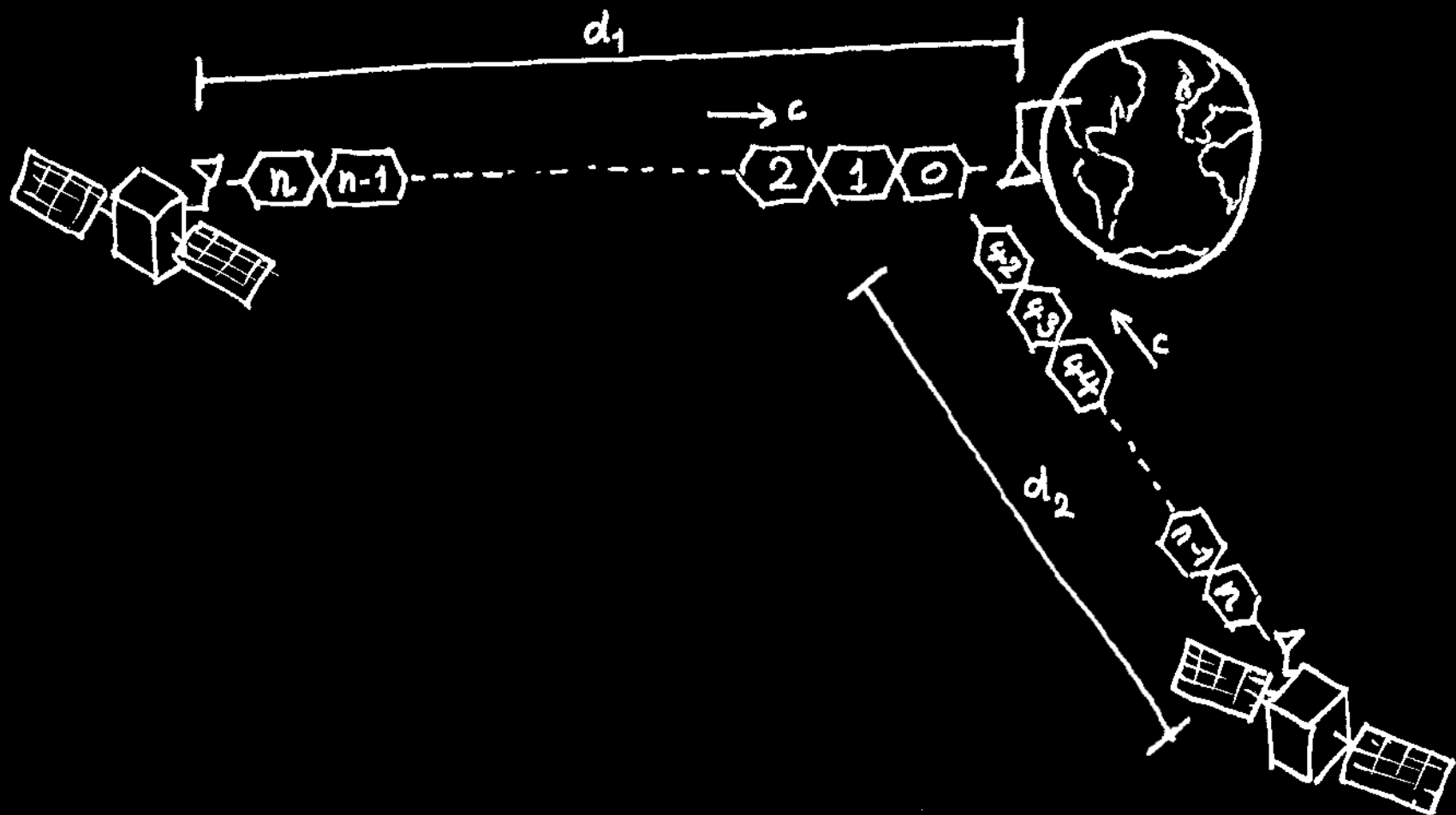


Weatherproof design,  
sealed connectors

38,300

Appendix





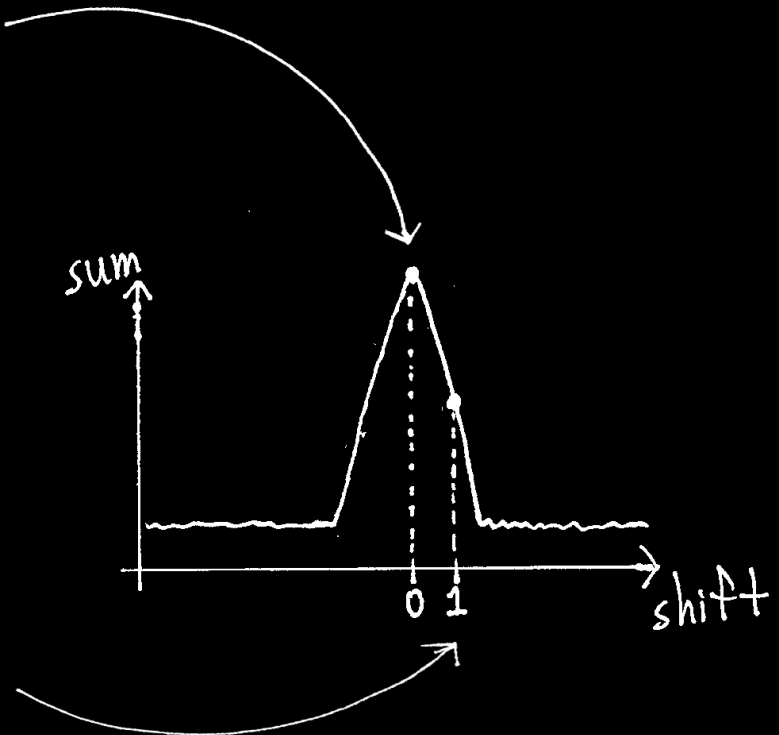
# Measuring the code phase

$$\begin{array}{r}
 \boxed{-} \boxed{+ + +} \boxed{-} \boxed{+} \boxed{-} \boxed{+} \\
 \boxed{-} \boxed{+ + +} \boxed{-} \boxed{+} \boxed{-} \boxed{+} \\
 \hline
 + + + + + + + + \\
 \text{sum} = 8
 \end{array}$$

shift = 0

$$\begin{array}{r}
 \boxed{-} \boxed{+ + +} \boxed{-} \boxed{+} \boxed{-} \boxed{+} \\
 \boxed{+} \boxed{-} \boxed{+ + +} \boxed{-} \boxed{+} \boxed{-} \\
 \hline
 \boxed{-} \boxed{-} \boxed{+ +} \boxed{-} \boxed{-} \boxed{-} \boxed{-} \\
 \text{sum} = -4
 \end{array}$$

shift = 1



# Measuring the code phase

Received  $\overline{-} \overline{+ + +} \overline{-} \overline{+} \overline{-} \overline{+}$   
 Locally Generated  $\overline{-} \overline{+ + +} \overline{-} \overline{+} \overline{-} \overline{+}$   $\text{shift} = 0$   

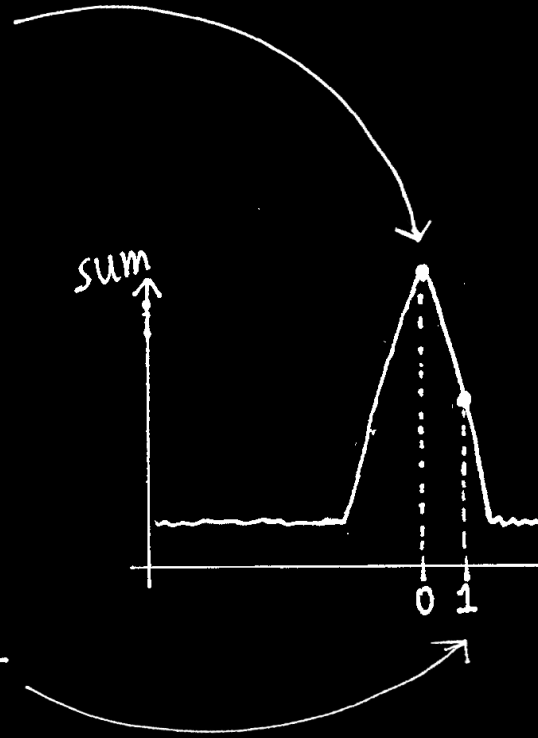

---

 Result  $\overline{+ + + + + + + +}$   $\text{sum} = 8$

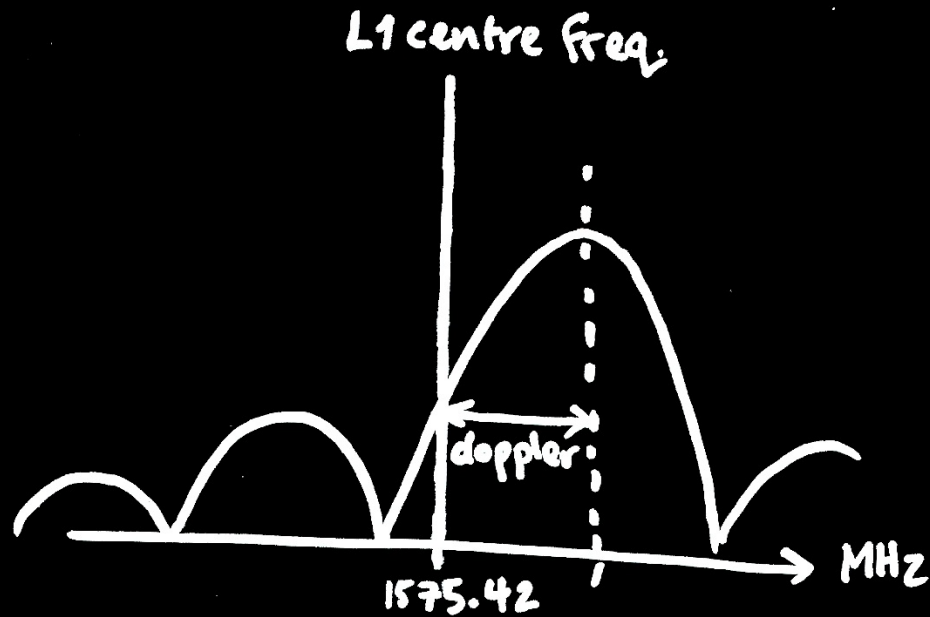
Received  $\overline{-} \overline{+ + +} \overline{-} \overline{+} \overline{-} \overline{+}$   
 Locally Generated  $\overline{+} \overline{-} \overline{+ + +} \overline{-} \overline{+} \overline{-}$   $\text{shift} = 1$   


---

 Result  $\overline{- -} \overline{+ +} \overline{- - - -}$   $\text{sum} = -4$

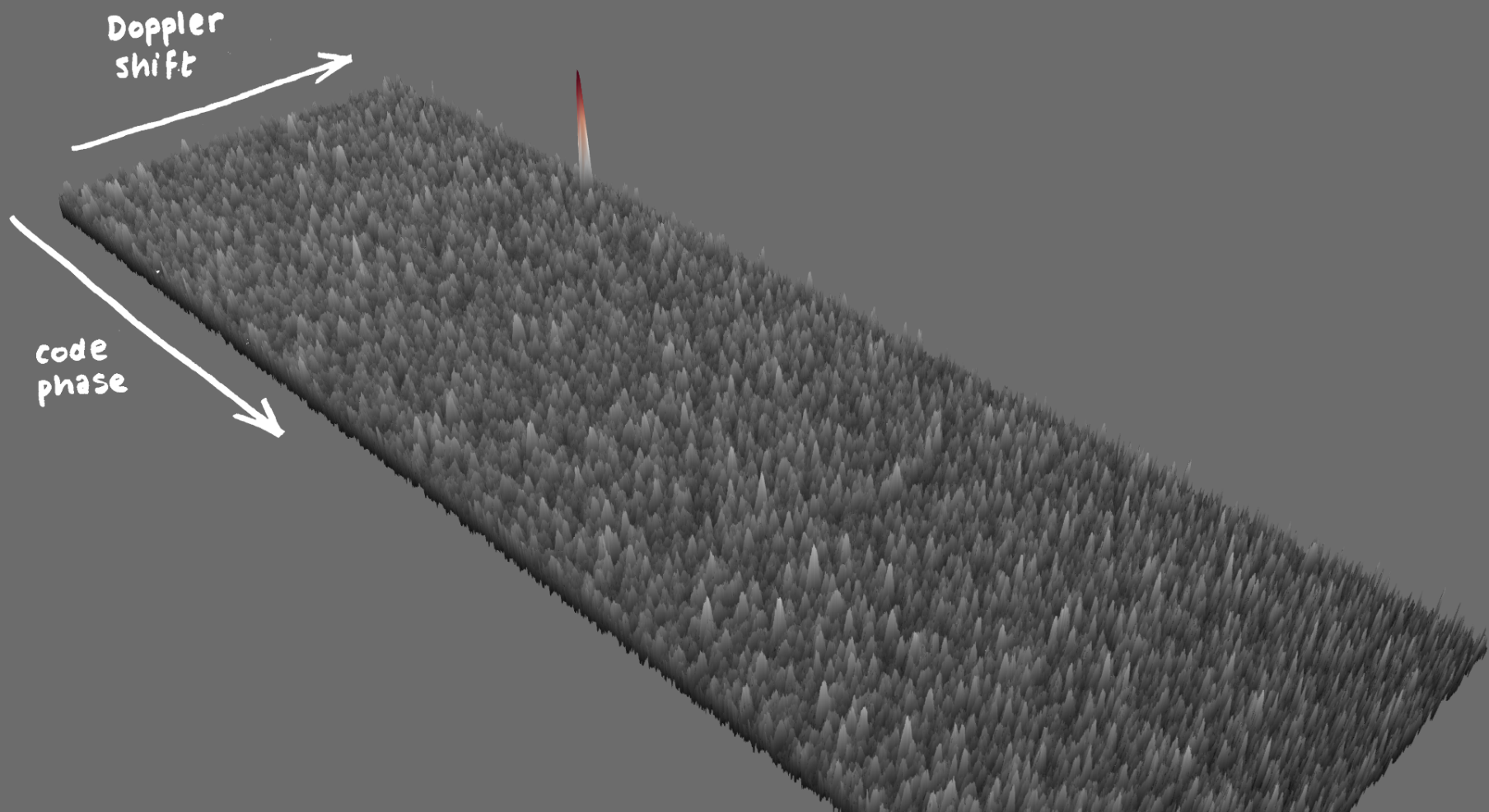


# Doppler shift

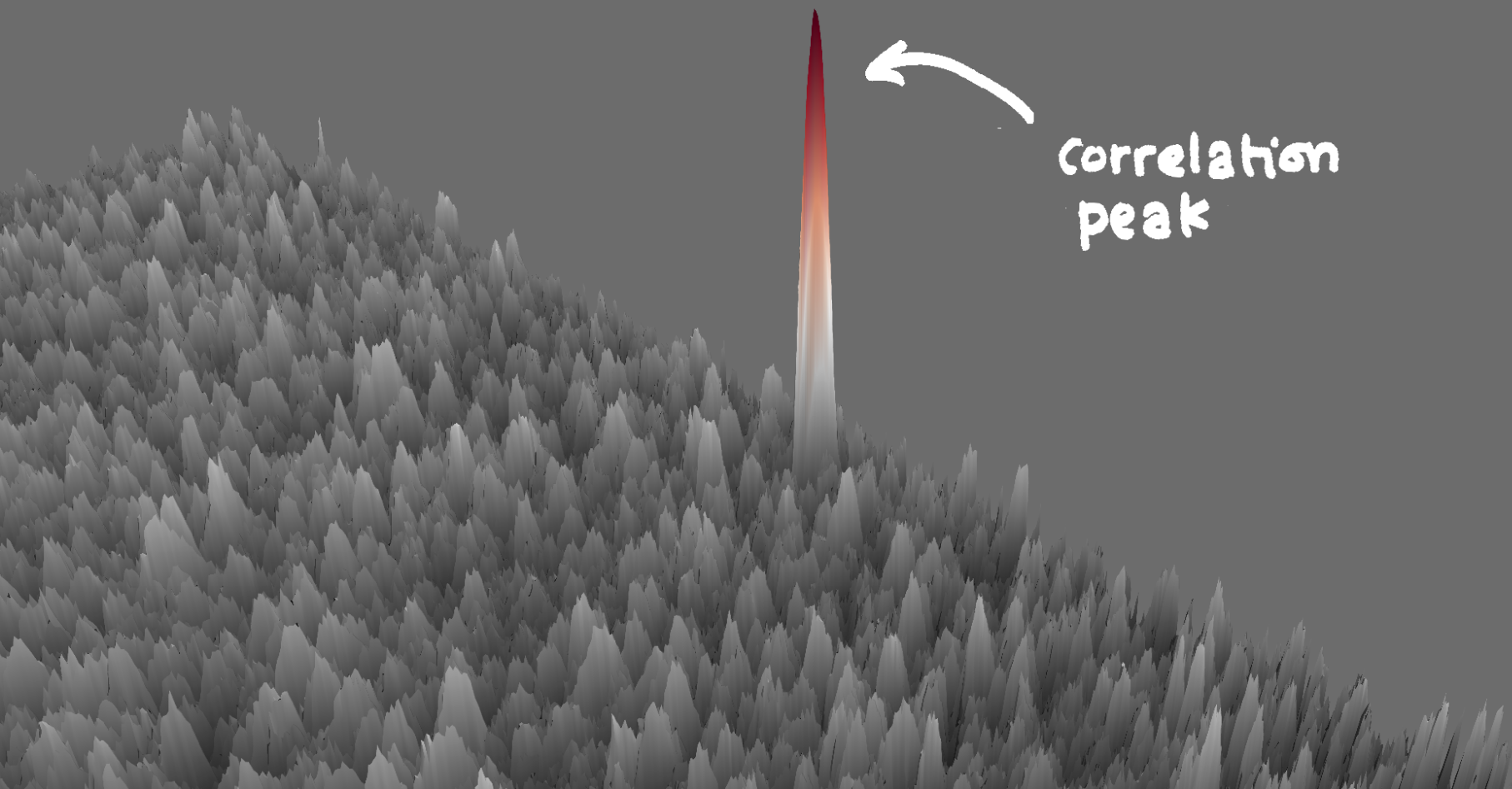


Acquisition

# Acquisition



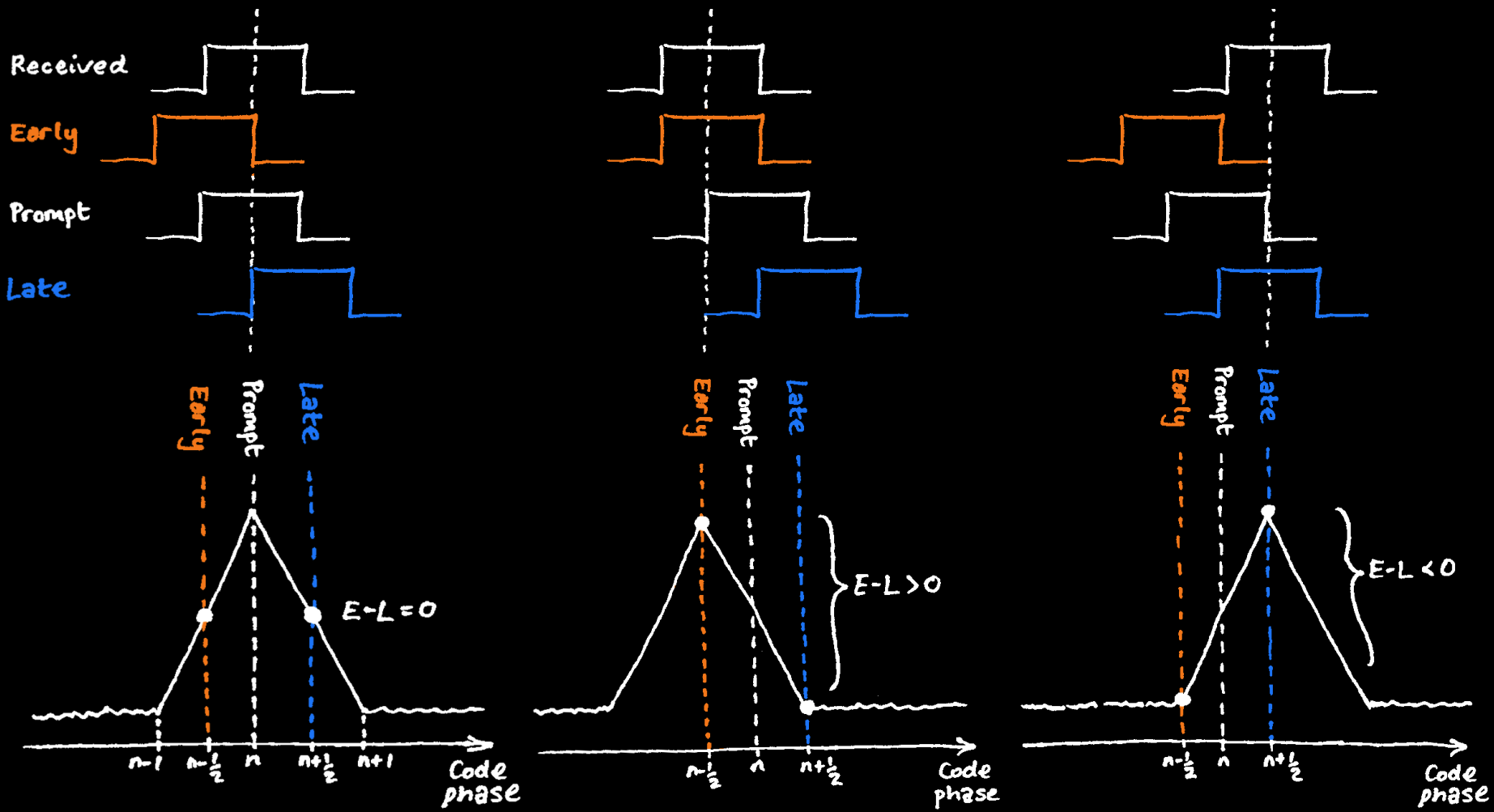
# Acquisition



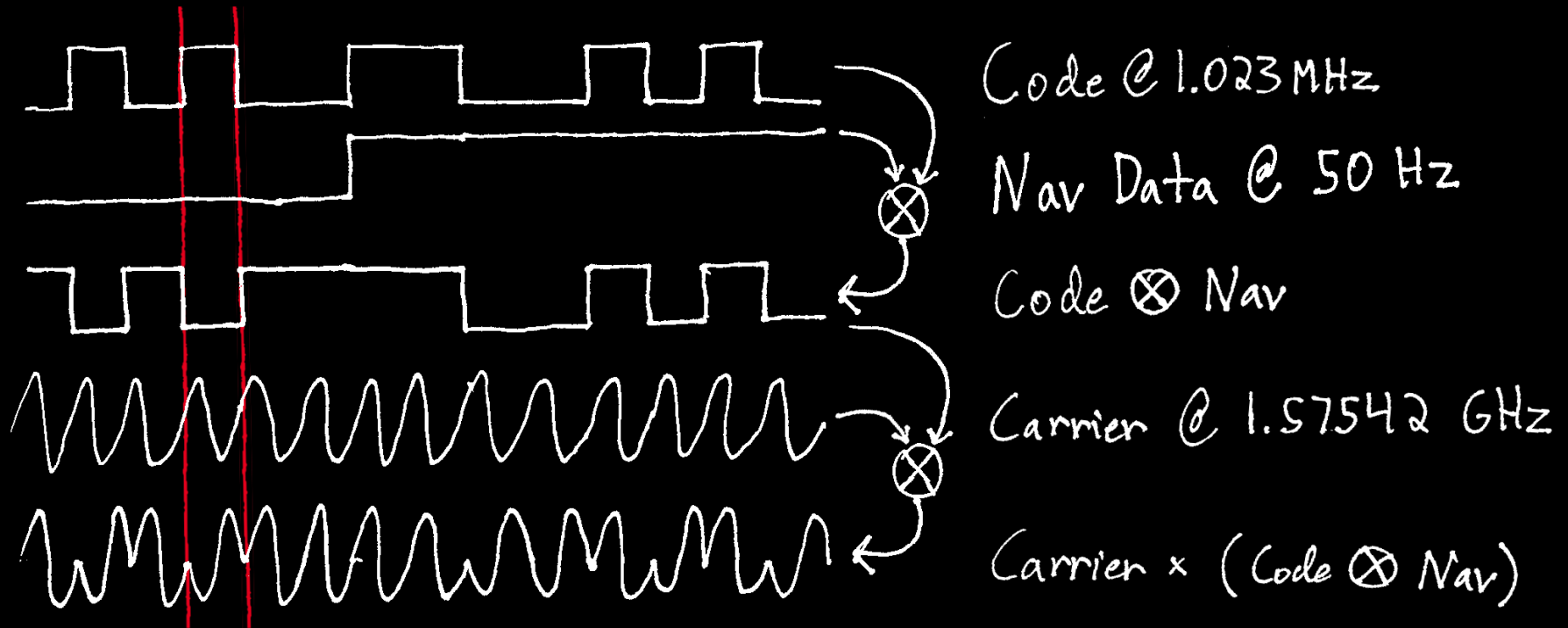
Tracking



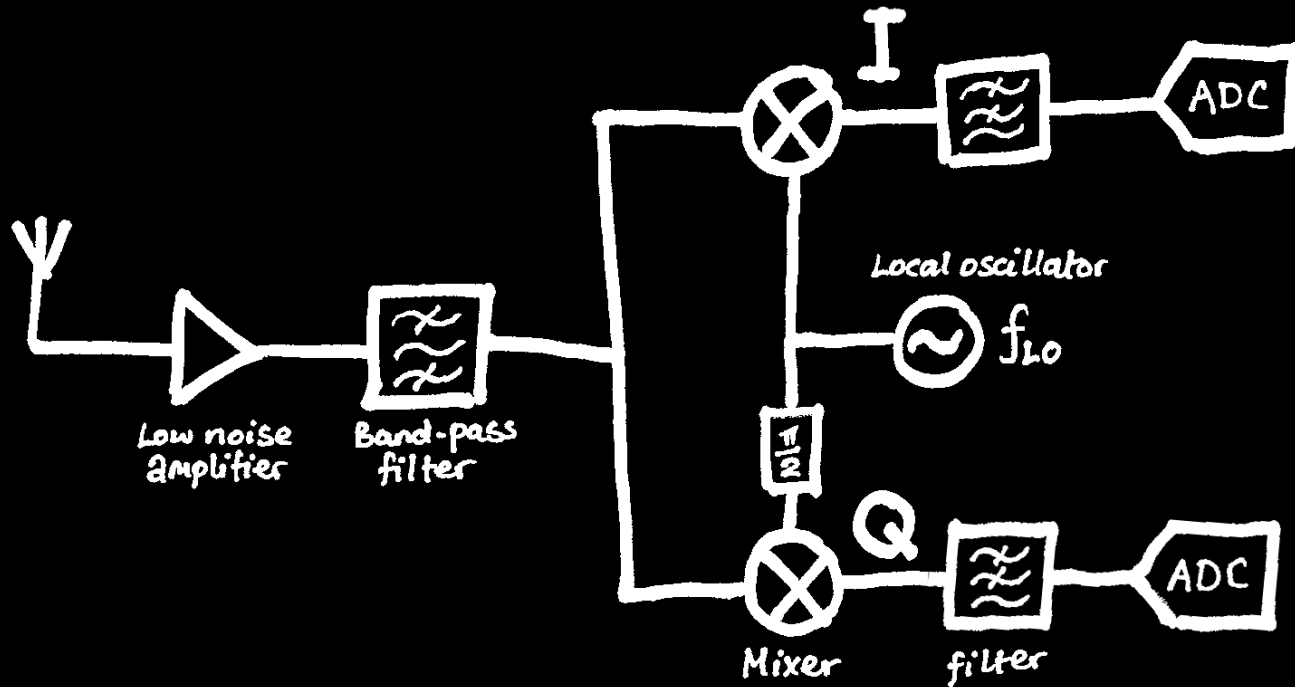
# Tracking



# Signal structure



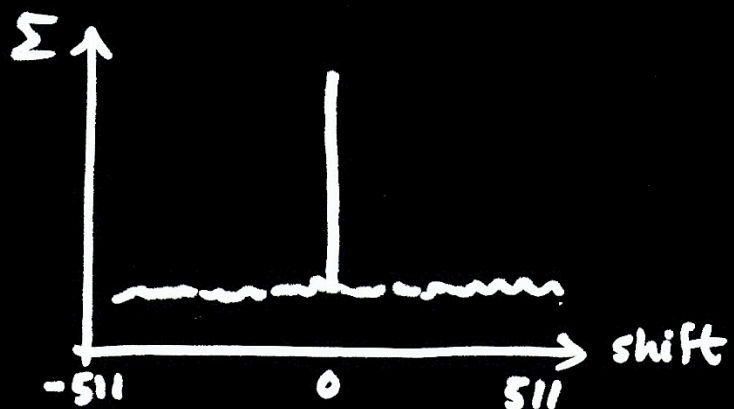
# Analog Frontend



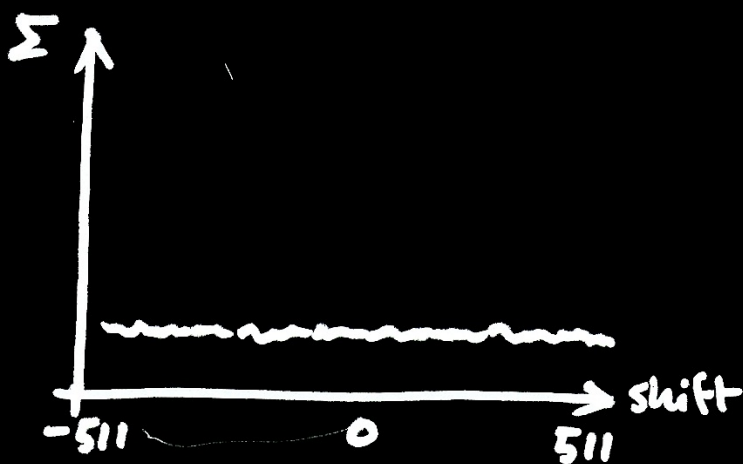
$$\cos \theta \cos \phi = \frac{\cos(\theta - \phi) + \cos(\theta + \phi)}{2}$$

# Gold codes

$$\text{length} = 2^n - 1$$

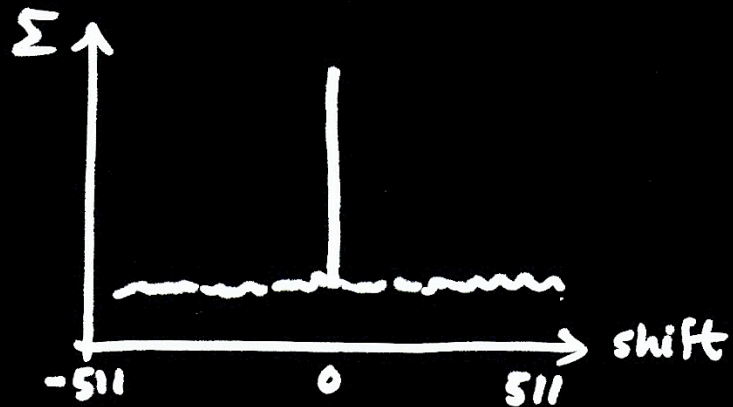


Auto correlation

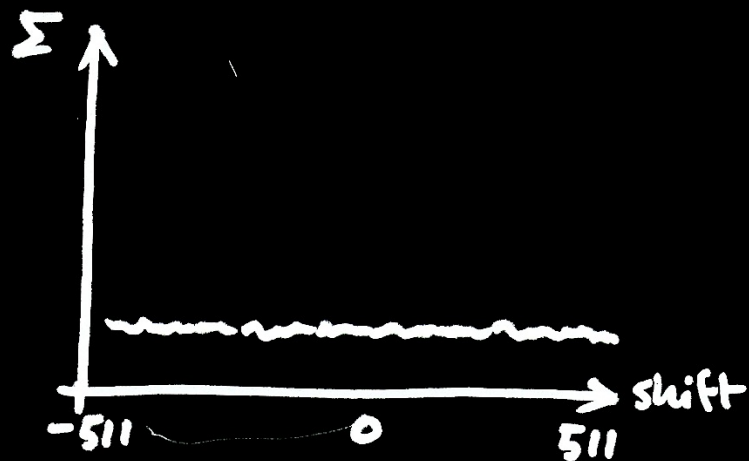


Cross-correlation

# Receiving from multiple satellites



sat A code \* sat A code



sat A code \* sat B code